## 2.5

Proofs About
Angle Pairs and Segments
(Day 2)


What would you conjecture is the relationship between two angles that are complements to the same angle?


Is this conjecture something we accept as true as a postulate?
Or can we prove it to be a theorem with previous knowledge?

Given: $\angle 1 \& \angle 2$ are complementary $\angle 3 \& \angle 2$ are complementary

Prove: $\angle 1 \cong \angle 3$

| Statement |
| :--- |
| 1. $\angle 1 \& \angle 2$ are complementary |
| $\angle 3 \& \angle 2$ are complementary |
| 2. $m \angle 1+m \angle 2=90$ |
| $m \angle 3+m \angle 2=90$ |
| 3. $m \angle 1+m \angle 2=m \angle 3+m \angle 2$ |
| 4. $m \angle 1=m \angle 3$ |
| 5. $\therefore \angle 1 \cong \angle 3$ |



## Congruent Complements Theorem ${ }^{\text {PoK }} 3$



If two angles are to the $\qquad$ then they are congruent.

What would you conjecture is the relationship between two angles that are supplements to the same angle?


Is this conjecture something we accept as true as a postulate?
Or can we prove it to be a theorem with previous knowledge?

Given: $\angle 1 \& \angle 2$ are supplementary $\angle 3 \& \angle 2$ are supplementary

Prove: $\angle 1 \cong \angle 3$


## Congruent Supplements Theorem pok <br>  <br> 

If two angles are to the then they are congruent.

## Linear Pair Postulate $\sum$ pok $\}$



If two angles form a linear pair, then they are supplementary

## Vertical Angles

Two angles across from each other from the vertex, when two lines cross.


What would you conjecture is the relationship between vertical?

Leave as postulate? Prove as theorem?

Given: $\angle 1 \& \angle 3$ are vertical angles
Prove: $\angle 1 \cong \angle 3$


1. $\angle 1 \& \angle 3$ are vertical angles
2. $\angle 1 \& \angle 2$ are a linear pair
$\angle 2 \& \angle 3$ are a linear pair
3. $\angle 1 \& \angle 2$ are supplementary
$\angle 2 \& \angle 3$ are supplementary
4. $\therefore \angle 1 \cong \angle 3$

## Vertical Angles (VA) Theorem $\underset{\sim}{\text { Pouk }} \stackrel{\substack{ \\\sim}}{\substack{2}}$



If they are

## Application:

If the measure of $m \angle 1$ is $5 w+3$ and $m \angle 3$ is $98^{\circ}$, find the measure of all the angles.


